

13 Free Cheatsheets!

Year 11 **MATHS METHODS**
Unit 1 & 2

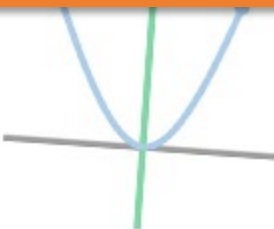
FREE Overview_{v1.98}

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$$f(-x) = f(x)$$



Purpose of this book

Hello!

This is a brief overview of *Units 1 & 2 Mathematical Methods* to help you learn and revise more efficiently. It is essentially a cut down version of the *Units 3 & 4 Overview*.

It was originally designed as a reference book for students who use the *online video tutorials* on **MathsMethods.com.au** but has since been used by many as their Bound Reference. Each page has a [clickable link](#) to direct you to the relevant video tutorial if you have access and there's plenty of other [free resources](#) if you don't!

Please note, like many of our resources, this overview is designed to reinforce *understanding* and may not use the exact notation you need to use when doing tests and exams.

Do well and I hope this overview makes the year a little less stressful for you :)

Kind regards

A handwritten signature in black ink, appearing to read 'Alex Bell'.

Alexander Bell | Author & Founder of **MathsMethods.com.au**

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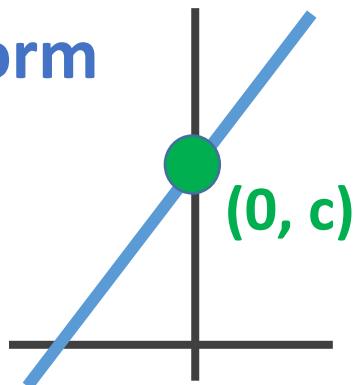
Covered in detail in video tutorials, see [LINEAR EQUATIONS](https://www.mathsmethods.com.au/linear-equations)

Gradient-Intercept Form

$$y = mx + c$$

m means gradient

c means y-intercept

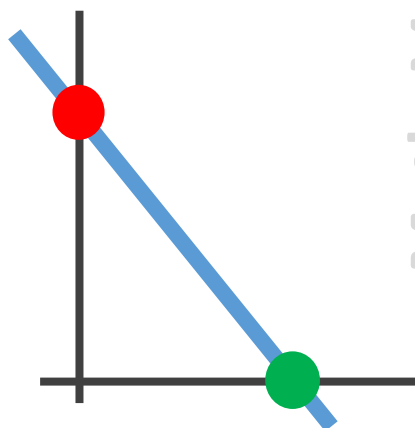


Intercept Form

$$ax + by = c$$

To find **x-intercept**, make $y = 0$

To find **y-intercept**, make $x = 0$

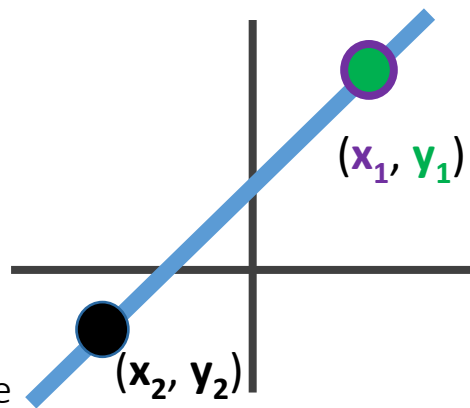


Two point Form

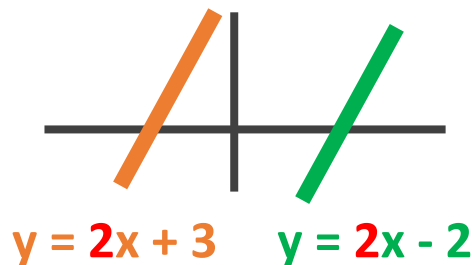
$$y - y_1 = m(x - x_1)$$

(x_1, y_1) is any point on the line

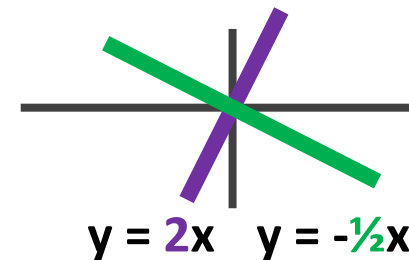
(x_2, y_2) is any *different* point on the line



Parallel means the same **gradient**



Perpendicular means $m = \frac{-1}{m}$



Simultaneous equations means solving two or more equations at the same time.

$$y = x$$

$$y = 4 - x$$

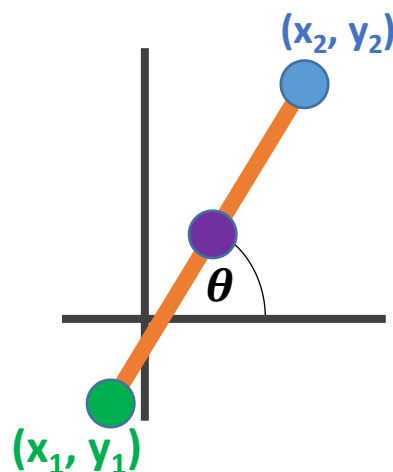
Substitution

$$y = x$$

$$y = 4 - x$$

Elimination

$$y + y = \cancel{x} + 4 - \cancel{x}$$



Length of line Segment = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

Co-ordinate of Midpoint = $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$

$$\theta = \tan^{-1}(\text{gradient})$$

$$\text{gradient} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\text{rise}}{\text{run}}$$

Want **FREE RESOURCES** on this topic? See [LINEAR EQUATIONS \(FREE VIDEO SERIES\)](https://www.mathsmethods.com.au/linear-equations)

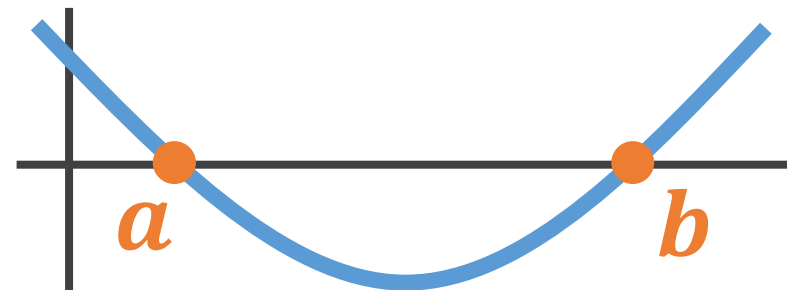
For more resources, see [MathsMethods.com.au](https://www.mathsmethods.com.au)

Covered in detail in video tutorials, see [PARABOLAS & QUADRATICS](https://www.mathsmethods.com.au/parabolas/)

Intercept Form

$$y = d(x - a)(x - b)$$

1. See if positive or negative
2. Draw in x intercepts (which are a and b)
3. Find y intercept (make $x = 0$)

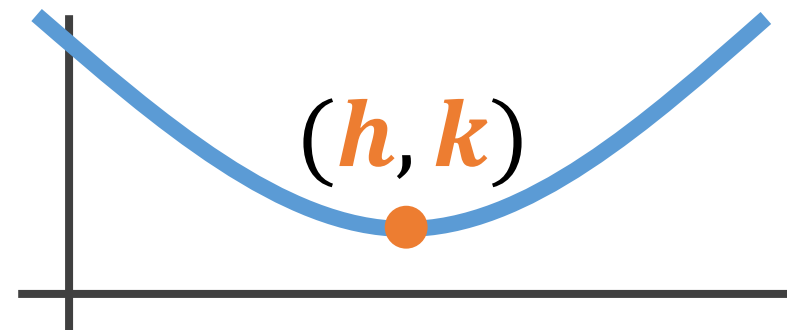


Turning Point Form

$$y = a(x - h)^2 + k$$

1. See if positive or negative
2. Draw in turning point (h, k)
3. Find intercepts (make $x = 0$ and then $y = 0$)

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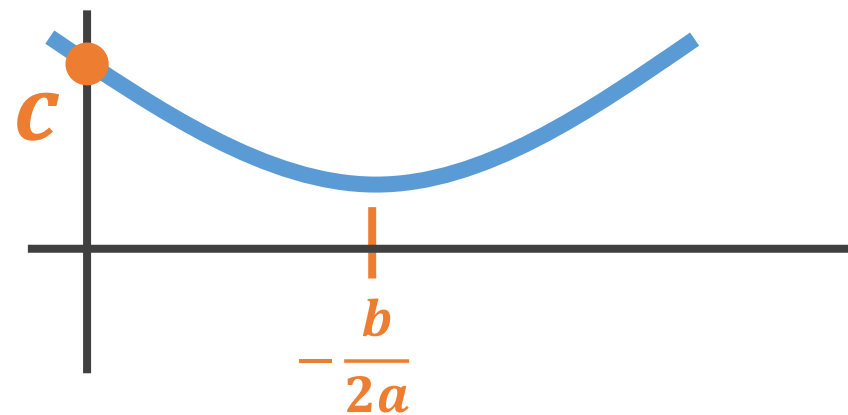


General Form

$$y = ax^2 + bx + c$$

1. See if positive or negative
2. Draw in y-intercept
3. Find x-intercepts if there are any
4. Find turning point

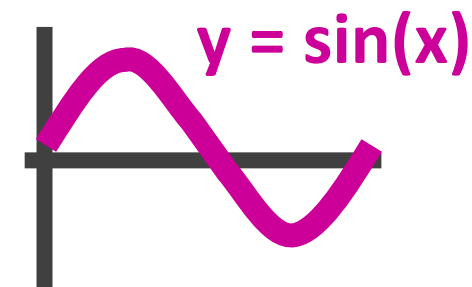
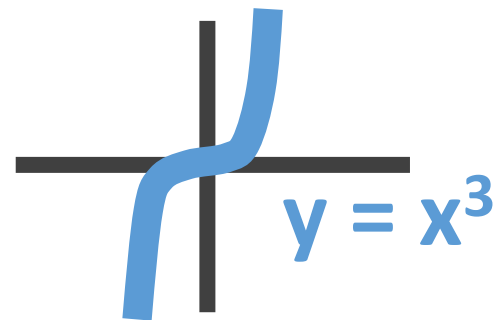
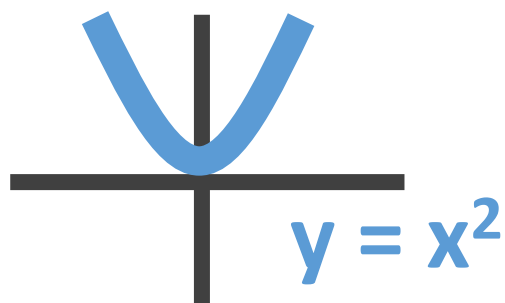
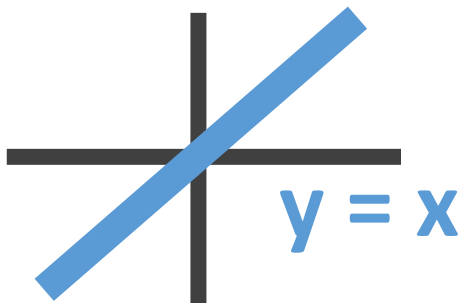
$$x \text{ intercepts} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$



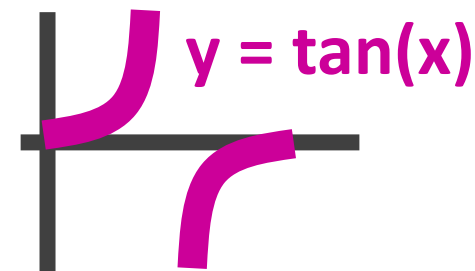
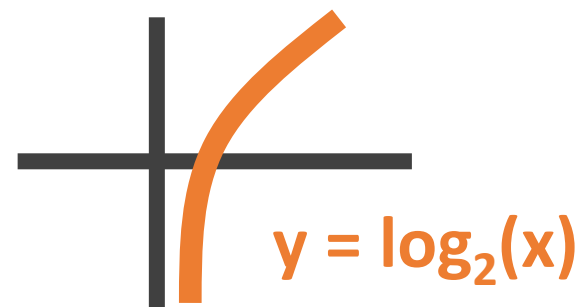
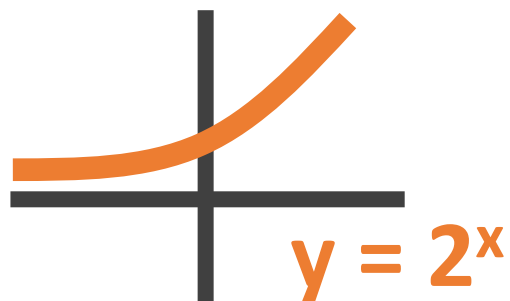
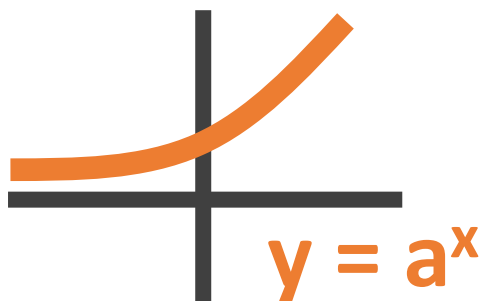
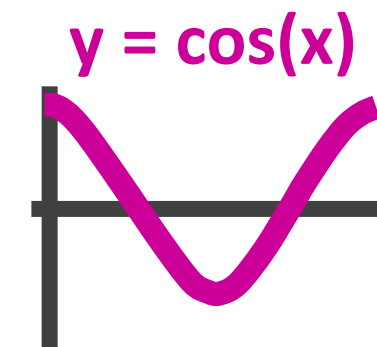
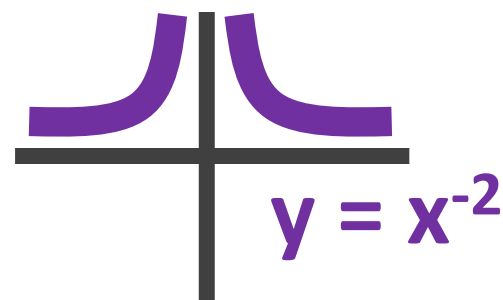
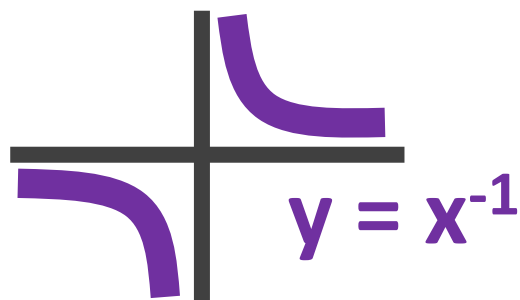
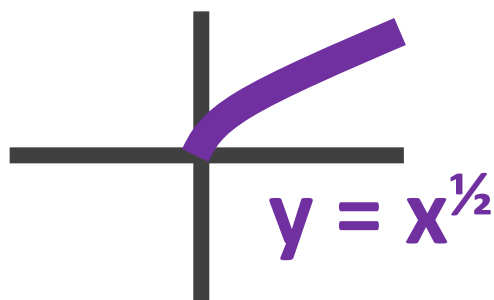
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For more resources, see [MathsMethods.com.au](https://www.mathsmethods.com.au)

Covered in detail in video tutorials, see [HOW TO SKETCH ANY FUNCTION](#)



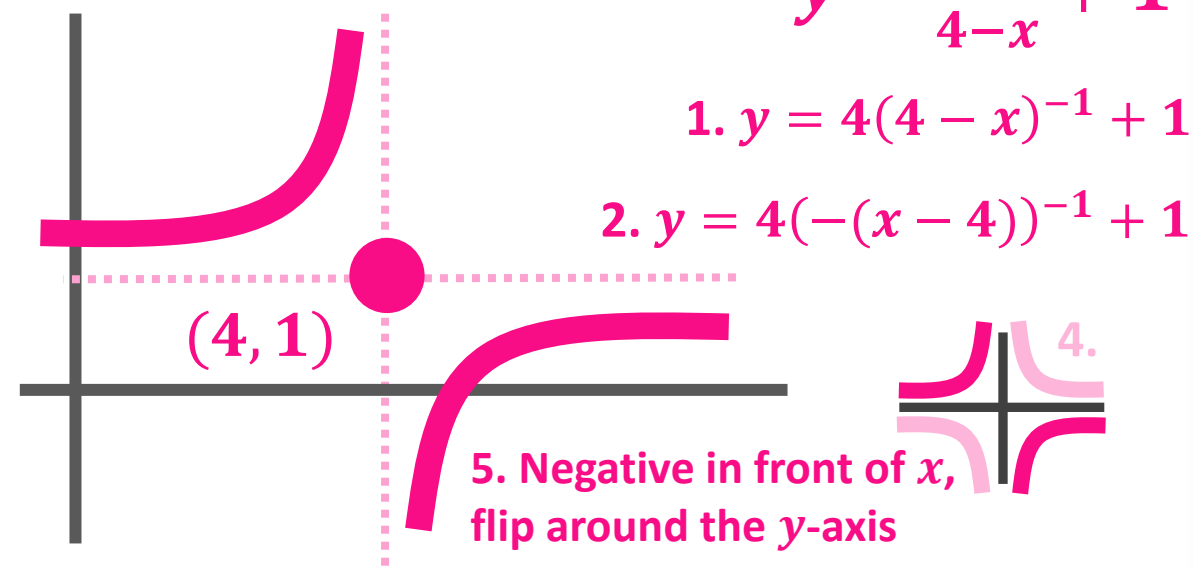
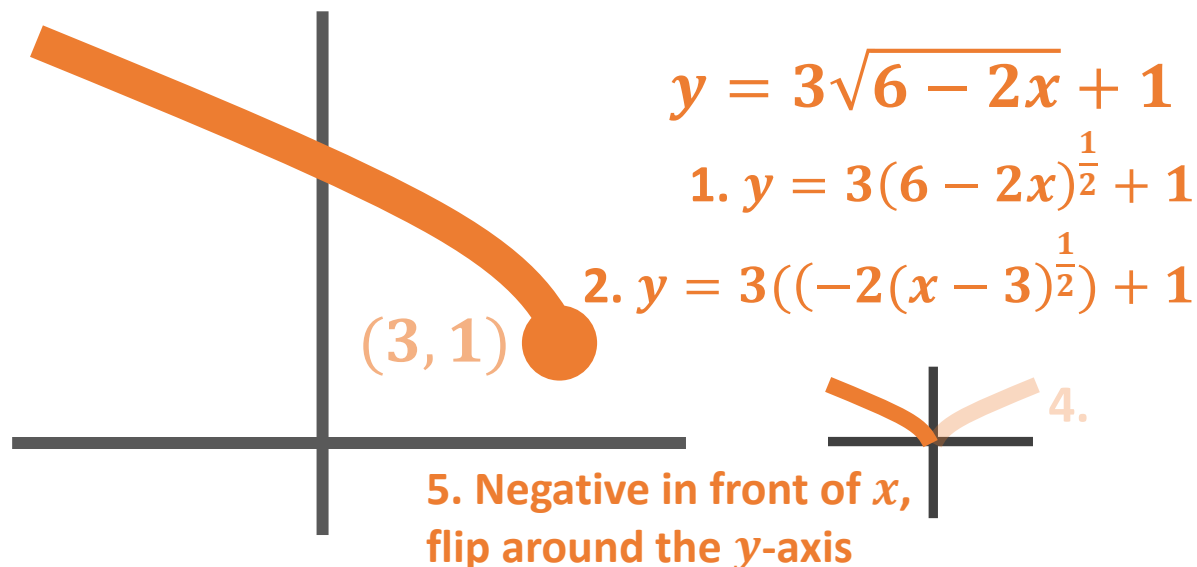
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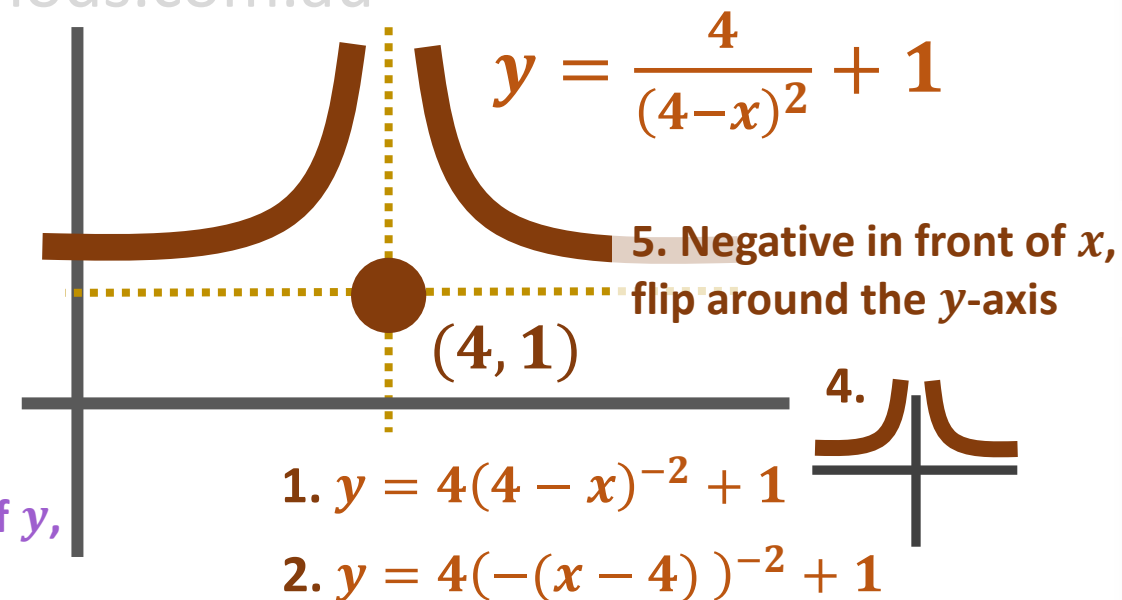
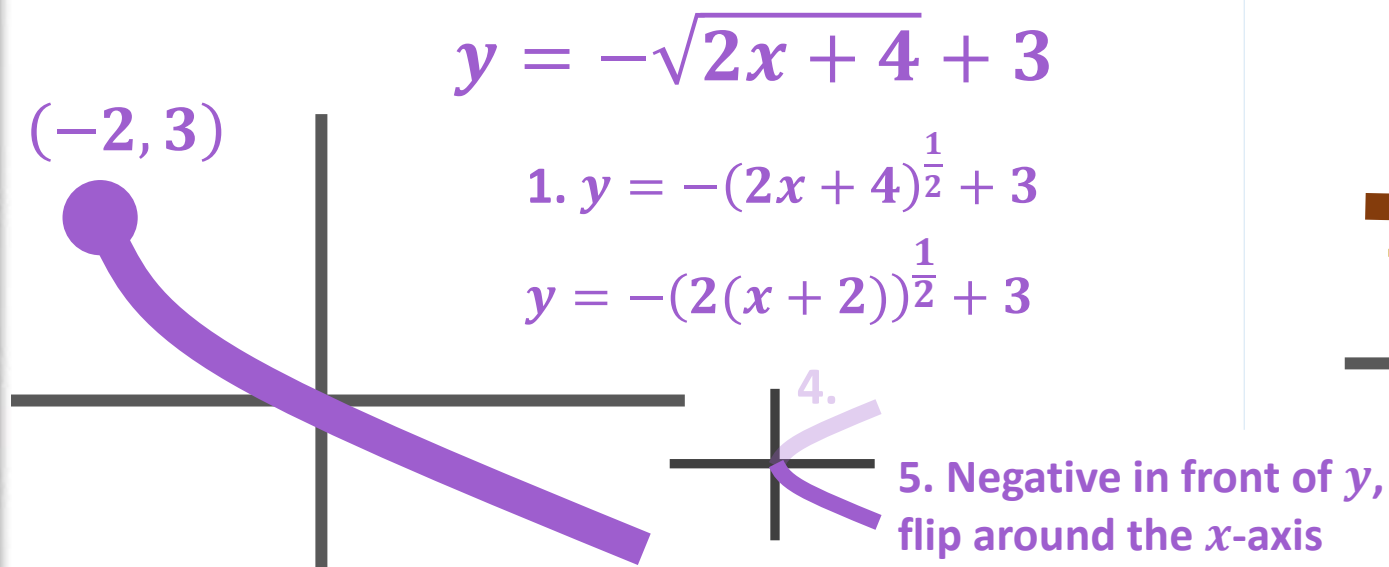
5 STEPS: 1. Change form 2. Factorise inside 3. Turning Point 4. Shape 5. Reflections

Covered in detail in video tutorials, see [TRANSLATION – MOVING FUNCTIONS](#) and [STRETCHING AND REFLECTING](#)

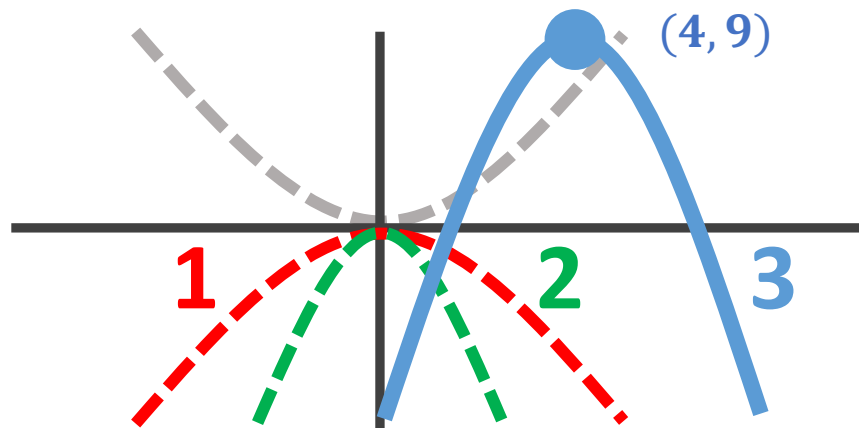
$$y = \frac{4}{4-x} + 1$$



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Covered in detail in video tutorials, see [FUNCTIONS AND POINTS](#), [USING MATRICES](#) and [SERIES OF TRANSFORMATIONS](#)



$$x^2 \rightarrow -(2(x-4))^2 + 9$$

$$-f(x) = -x^2$$

1. Reflection in the x-axis

$$f(2x) = -(2x)^2$$

2. Followed by a dilation of factor $\frac{1}{2}$ from the y-axis

$$f(x-4) + 9 = -(2(x-4))^2 + 9$$

3. Then a translation of 4 units in positive x-direction and 9 units in the positive y-direction

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$f\left(\frac{1}{a}x\right)$ is a dilation of factor **a** from the y-axis
(in the x-direction)

$f(-x)$ is a reflection in the y-axis

$-f(x)$ is a reflection in the x-axis

b $f(x)$ is a dilation of factor **b** from the x-axis
(in the y-direction)

$f(x) + k$ is a translation along the y-axis

$f(x - h)$ is a translation along the x-axis

Positive
Power

$$x^2 = 1 \times x \times x$$

$$x^1 = 1 \times x$$

$$x^0 = 1$$

Covered in detail in video tutorials, see [EXPONENTIAL LAWS \(POWER LAWS\)](#)

Negative
Power

$$\frac{x^m}{x^n} = x^{m-n}$$

$$x^{-1} = \frac{1}{x}$$

$$x^{-n} = \frac{1}{x^n}$$

Fraction
Power

$$x^{\frac{1}{2}} = \sqrt{x}$$

$$x^{\frac{1}{m}} = \sqrt[m]{x}$$

$$x^{\frac{m}{n}} = \sqrt[n]{x^m}$$

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$$x^m x^n = x^{m+n}$$

$$(x^m)^n = x^{mn}$$

$$\left(\frac{x}{y}\right)^n = \frac{x^n}{y^n}$$

Log is power

$$\log_2 8 = 3$$

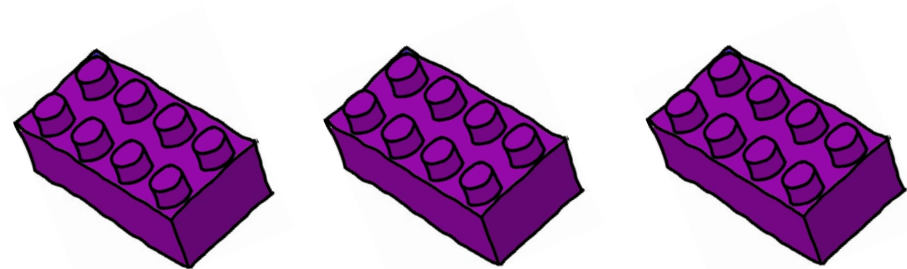
How many 2s are
multiplied together

$$2^3 = 8$$

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Logarithm is a Greek word

Logos means how many there are



Arithmos means number

2

Logarithm originally means
how many numbers

$$y = -3e^{(2x+1)} - 2$$

1) Find any reflections

reflected in x-axis

2) Find asymptote

$$y = -2$$

3) Find intercepts

y-intercept, $x = 0$ no x-intercepts

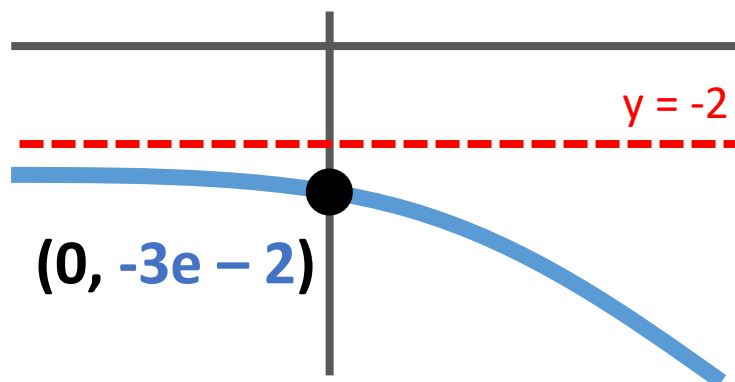
$$y = -3e^{2x+1} - 2$$

$$y = -3e^{2(0)+1} - 2$$

$$y = -3e^1 - 2$$

4) Domain **R**, Range **$(-\infty, -2)$**

Domain **R**, Range **$(-\infty, -2)$**



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$$y = \log_e(-2x + 4) - 3$$

1) Find any reflections

reflected in y-axis

2) Find asymptote

$$(-2x+4) = 0 \quad x = 2$$

3) Find intercepts

x-intercept, $y = 0$

y-intercept, $x = 0$

$$0 = \log_e(-2x + 4) - 3$$

$$y = \log_e(4) - 3$$

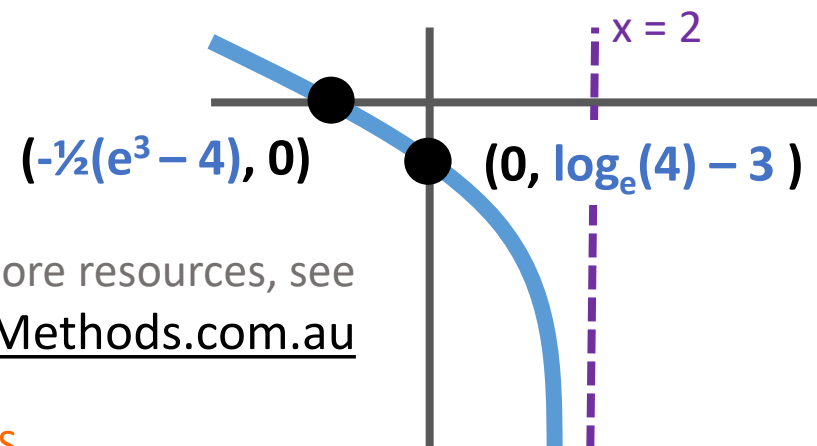
$$3 = \log_e(-2x + 4)$$

$$e^3 = -2x + 4$$

$$x = -\frac{1}{2}(e^3 - 4)$$

4) Domain **$(-\infty, 2)$** , Range **R**

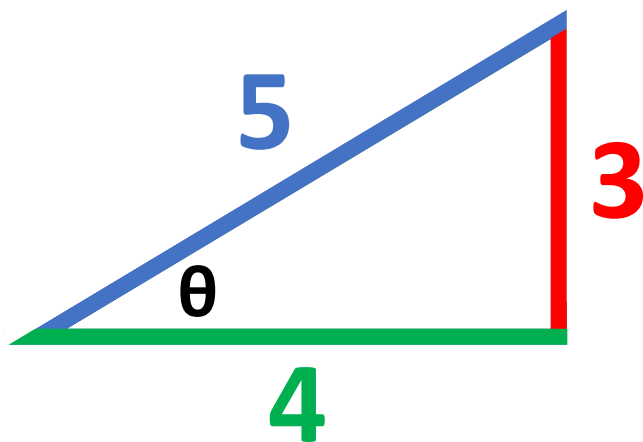
Domain **$(-\infty, 2)$** , Range **R**



For more resources, see
[MathsMethods.com.au](https://www.mathsmethods.com.au)

Covered in detail in video tutorials, see [DEFINITIONS OF SIN AND COS](#) and [THE UNIT CIRCLE](#)

SOH CAH TOA



$$\sin(\theta) = \frac{\text{Length of Opposite}}{\text{Length of Hypotenuse}} = \frac{3}{5}$$

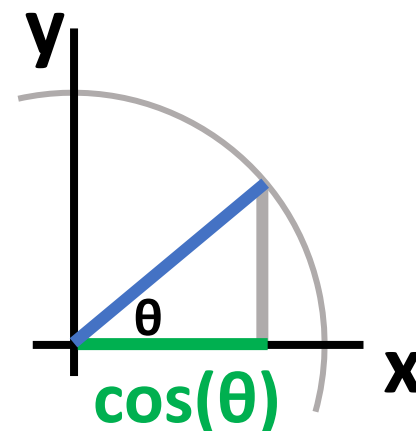
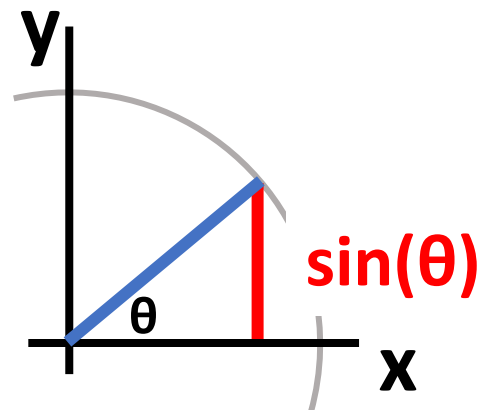
$$\cos(\theta) = \frac{\text{Length of Adjacent}}{\text{Length of Hypotenuse}} = \frac{4}{5}$$

$$\tan(\theta) = \frac{\text{Length of Opposite}}{\text{Length of Adjacent}} = \frac{3}{4}$$

In a unit circle, **hypotenuse** always = 1

$\sin(\theta)$ = Length of Opposite

$\cos(\theta)$ = Length of Adjacent

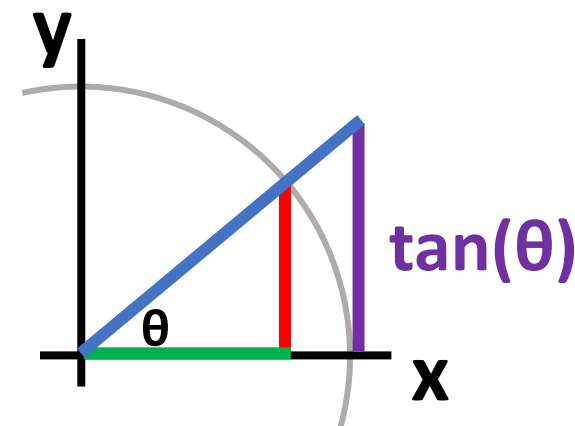


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Tangent is a line which touches a circle only at one point.

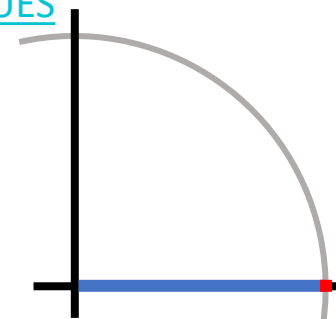


$\tan(\theta)$ is the length of the tangent, cut off by the x axis and the radius.

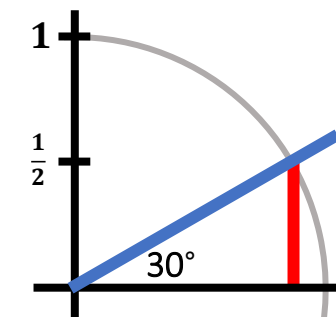


Covered in detail in video tutorials, see [PROVING EXACT VALUES](https://www.mathsmethods.com.au/proving-exact-values)

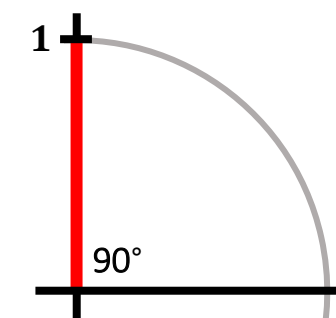
Angle	$\sin(\theta)$	$\cos(\theta)$	$\tan(\theta)$
0	0	1	0
$\frac{\pi}{6}$ 30	$\frac{1}{2}$	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{3}}$
$\frac{\pi}{4}$ 45	$\frac{\sqrt{2}}{2}$	$\frac{\sqrt{2}}{2}$	1
$\frac{\pi}{3}$ 60	$\frac{\sqrt{3}}{2}$	$\frac{1}{2}$	$\sqrt{3}$
$\frac{\pi}{2}$ 90	1	0	undefined



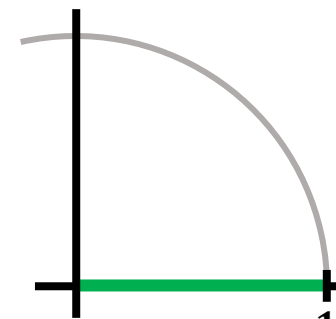
$$\sin(0) = 0$$



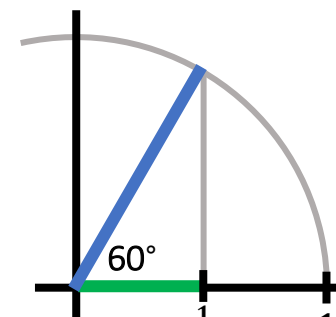
$$\sin(30) = \frac{1}{2}$$



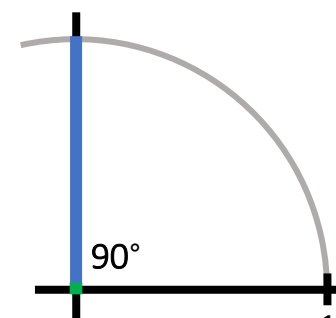
$$\sin(90) = 1$$



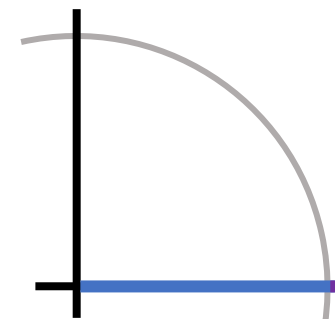
$$\cos(0) = 1$$



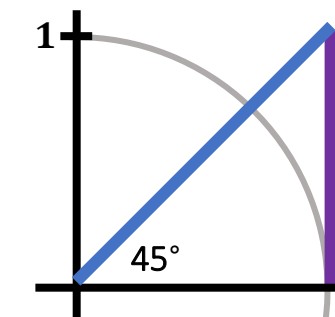
$$\cos(60) = \frac{1}{2}$$



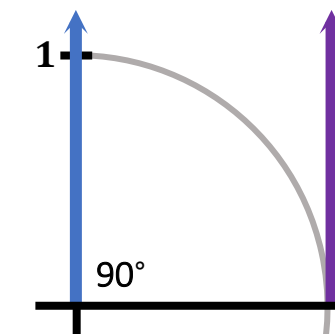
$$\cos(90) = 0$$



$$\tan(0) = 0$$



$$\tan(45) = 1$$



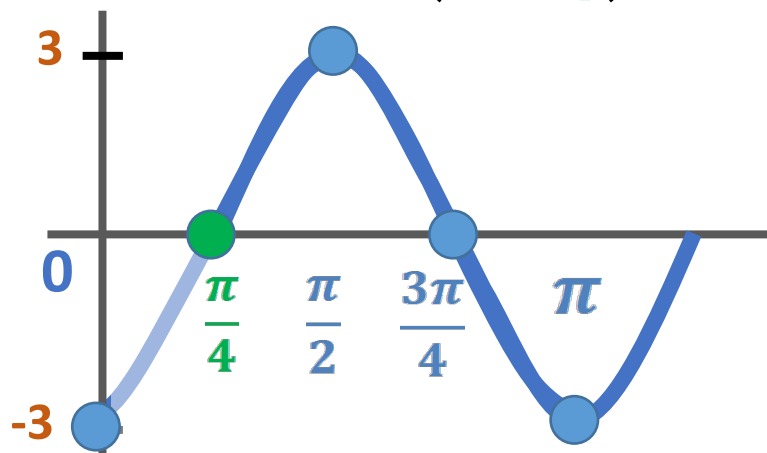
$$\tan(90) = \text{undefined}$$

Graphing **SIN** or **COS** in *two* different formsCovered in detail in video tutorials, see [SKETCHING SIN, COS & TAN](#)

$$y = A \sin(k(x - b))$$

1. Draw in **starting point** and **amplitude**
2. Period = $\frac{2\pi}{k} = \pi$
3. Divide period into 4 = $\frac{\pi}{4}$
4. Add and subtract this to **starting point**

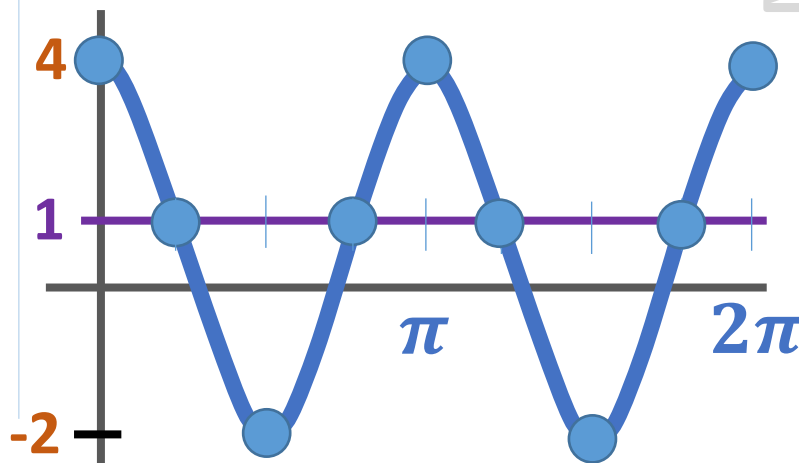
$$y = 3 \sin 2 \left(x - \frac{\pi}{4} \right)$$



$$y = A \sin(kx) + c$$

1. Draw in **vertical translation** and **A**
2. Period = $\frac{2\pi}{k} = \pi$
3. Write in period and divide it by 4
4. Find intercepts (see next page)

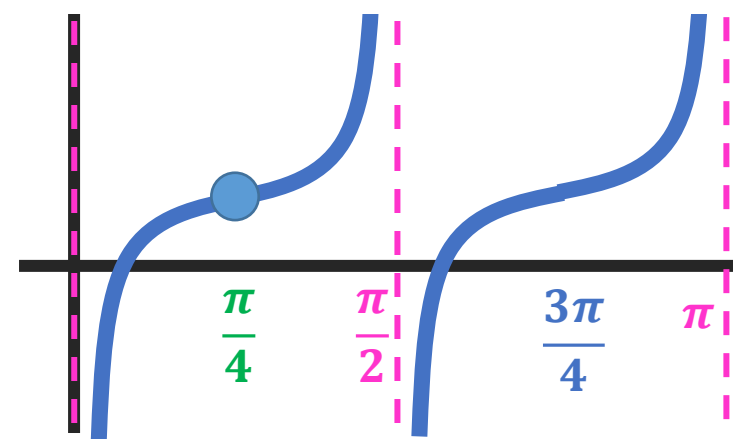
$$y = 3 \cos(2x) + 1$$

Graphing **TAN**

$$y = A \tan(k(x - b)) + c$$

1. Draw in starting point (**b**, **c**)
2. Period = $\frac{\pi}{k} = \frac{\pi}{2}$
3. Divide period into 2 = $\frac{\pi}{4}$
4. Add and subtract this to **starting point**
5. Draw in **asymptotes**

$$y = 3 \tan \left(2 \left(x - \frac{\pi}{4} \right) \right) + 1$$



Covered in detail in video tutorials, see [FINDING THE DERIVATIVE](#)

Derivative of x

$$f(x) = 5x^4 \quad f'(x) = 4 \times 5x^3$$

1. Multiply the x by the power
2. Minus one from the power

$$f(x) = \text{any number} \quad f'(x) = 0$$

example

$$f(x) = 6x^5 - 3x^{\frac{2}{3}} + 2x^{-1} - 4$$

$$f'(x) = 5 \times 6x^4 - \frac{2}{3} \times 3x^{-\frac{1}{3}} + -1 \times 2x^{-2} + 0$$

$$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx} \quad \text{is exactly the same as}$$

$$\frac{dy}{dx} = f'(g(x)) \times g'(x)$$

Chain Rule (short version)

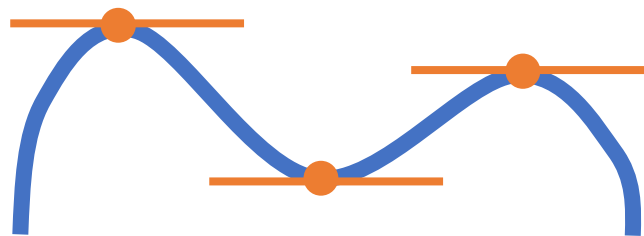
1. Derive outside function
2. Multiply it by derivative of the inside function

$$y = 2(x^3 - 5)^5$$

$$1. \quad 5 \times 2(x^3 - 5)^4$$

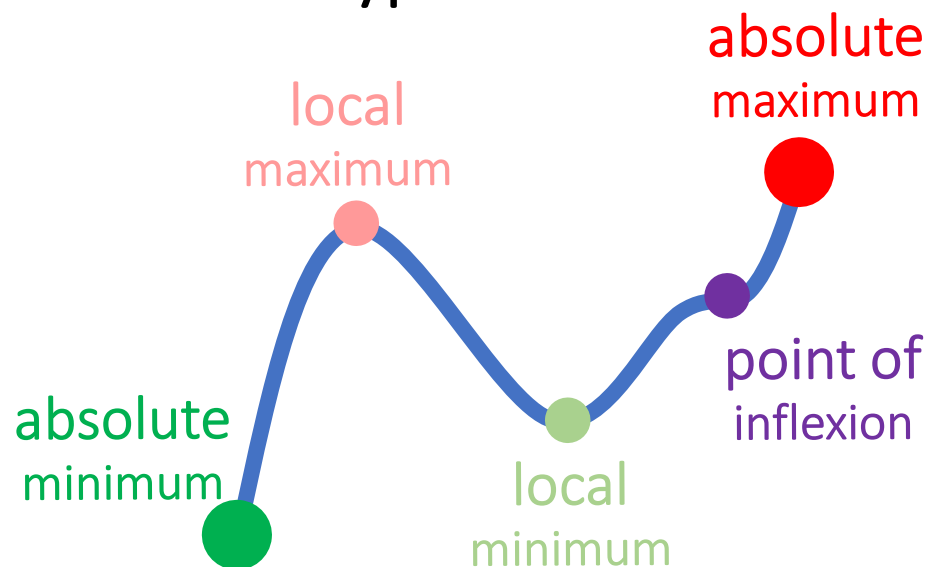
$$2. \quad \frac{dy}{dx} = 5 \times 2(x^3 - 5)^4 \times 3x^2$$

Stationary point means where the gradient of the curve is zero.



$$f'(x) = 0$$

Types of S.P



How to find stationary points $f(x) = 2x^3 + 1$

1. Find $f'(x) = 0$ and solve for x

$$f'(x) = 6x^2 \quad 6x^2 = 0 \quad x = 0$$

2. Sub x value into $f(x)$

$$f(0) = 2(0)^3 + 1 = 1$$

Stationary point
at $(0, 1)$

3. To find type: Sub in two x values (before and after the S.P.)

$$f'(-1) = 6(-1)^2 = 6$$

positive

$$f'(1) = 6(1)^2 = 6$$

positive

It is a point of infection (see diagram below)



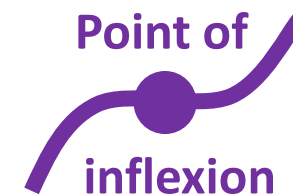
$$f'(\text{before}) = \text{positive}$$

$$f'(\text{after}) = \text{negative}$$



$$f'(\text{before}) = \text{neg}$$

$$f'(\text{after}) = \text{pos}$$



$$f'(\text{before}) = \text{pos}$$

$$f'(\text{after}) = \text{pos}$$

Kinematics is the subject about how objects move

x = displacement

$\frac{dx}{dt}$ = velocity

$\frac{dv}{dt}$ = acceleration

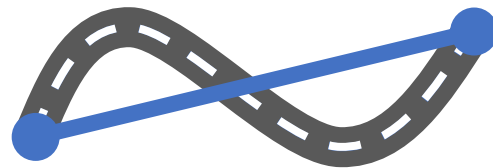
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Differentiate →

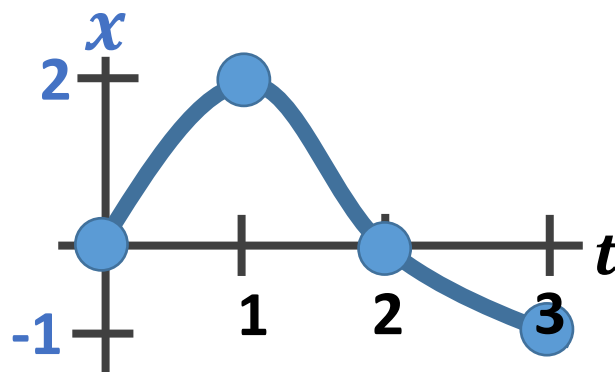
x $\frac{dx}{dt}$ $\frac{dv}{dt}$

← Antidifferentiate

Distance means how far something has moved



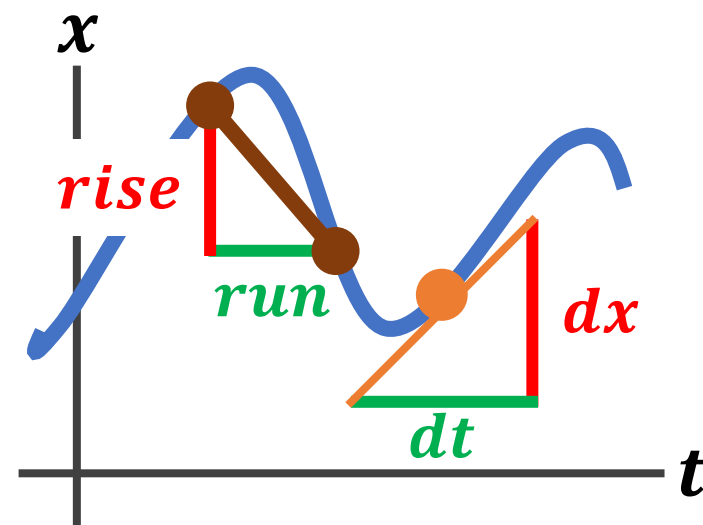
Displacement means how far away something is



time	0	1	2	3
Distance	0	2	4	5
Displacement	0	2	0	-1

Instantaneous means gradient

one point on the curve



Average means $\frac{\text{rise}}{\text{run}}$

two points on the curve

instantaneous velocity = $\frac{dx}{dt}$

average velocity = $\frac{\text{rise}}{\text{run}}$

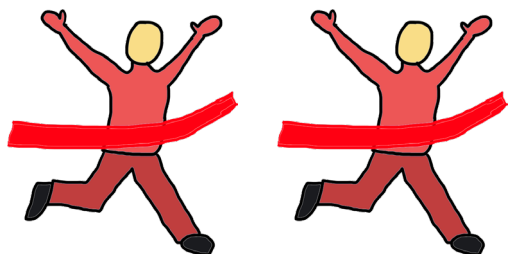
Covered in detail in video tutorials, see [RANDOM VARIABLES](#) and [DISCRETE RANDOM VARIABLES](#)

Discrete Random Variable is a letter that represents an outcome in terms of **countable** numbers

Usually use capital letter **X**

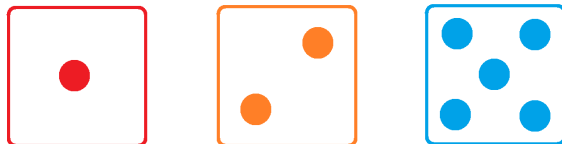
Races won (out of 3)

$\Pr(X = 2)$



Sum of a die when rolling 3 times

$\Pr(X = 8)$



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A few rules

If you add all the $\Pr(X)$, it will = 1

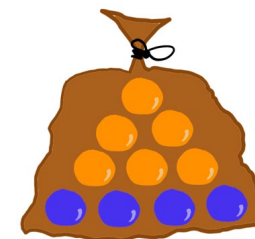
$\Pr(X = x)$ is **always positive** and **never larger than 1**

To find $\Pr(a \leq X \leq b)$, just add up all $\Pr(X)$ from a to b

Want **FREE RESOURCES** on this topic? See [DISCRETE RANDOM VARIABLES](#)

Example: 10 balls in a bag: 4 blue and 6 orange

If picking 3 balls at a time (with replacement), what is probability of only getting one blue ball?



Outcome	X	$\Pr(X)$
BBB	3	$0.4 \times 0.4 \times 0.4 = 0.064$
BBO	2	$0.4 \times 0.4 \times 0.6 = 0.096$
BOB	2	$0.4 \times 0.6 \times 0.4 = 0.096$
OBB	2	$0.6 \times 0.4 \times 0.4 = 0.096$
OOB	1	$0.6 \times 0.6 \times 0.4 = 0.144$
OBO	1	$0.6 \times 0.4 \times 0.6 = 0.144$
BOO	1	$0.4 \times 0.6 \times 0.6 = 0.144$
OOO	0	$0.6 \times 0.6 \times 0.6 = 0.216$

$$\Pr(X = 1) = 0.144 + 0.144 + 0.144 = 0.432$$

For more resources, see [MathsMethods.com.au](#)

Final thoughts & extra resources!

Hope you have enjoyed this material! If you have any comments or feedback, please feel free to contact me at alex@mathsmethods.com.au. Good luck!

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Kind regards



Alex Bell | Founder of **MathsMethods.com.au**

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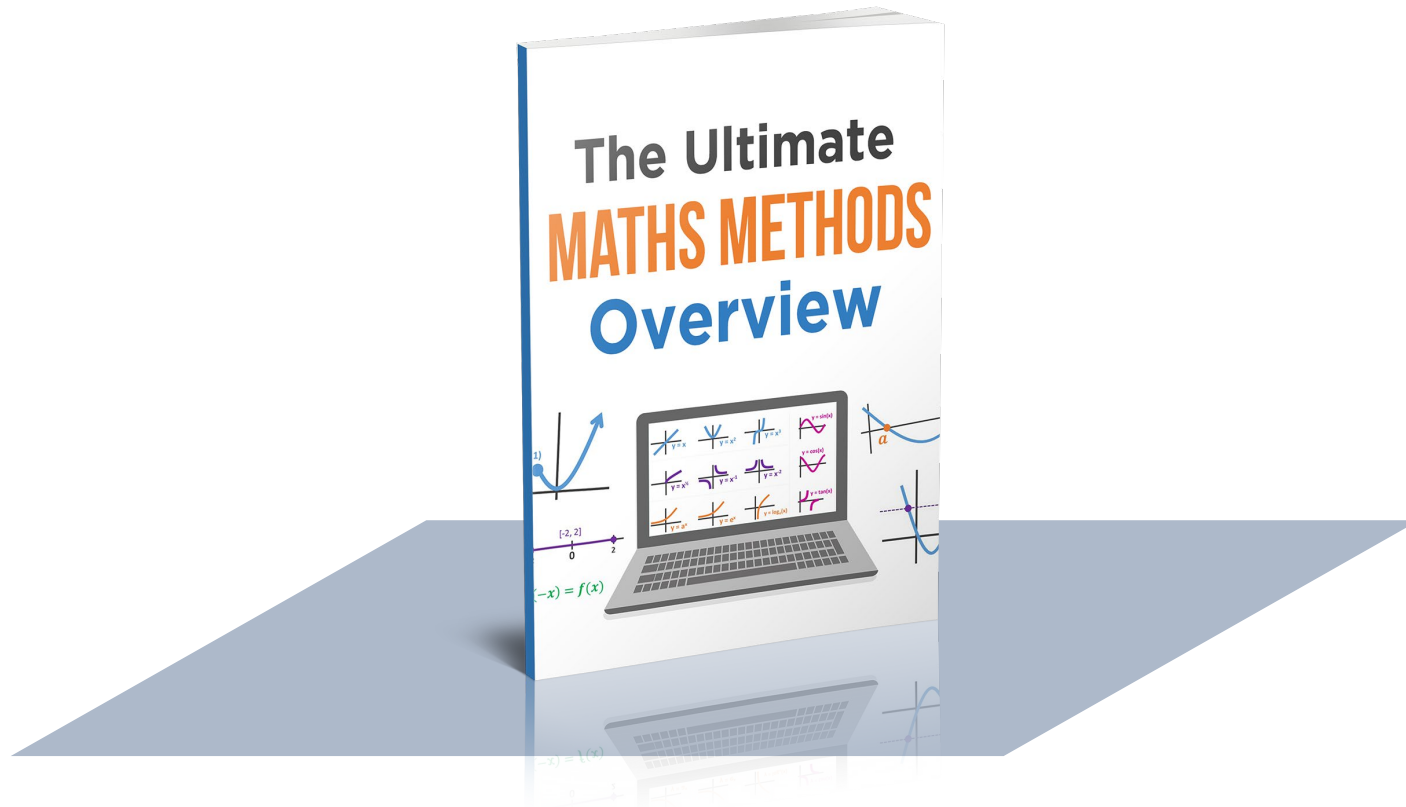
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